

Quiz 5
Chemical Engineering Thermodynamics
February 9, 2017

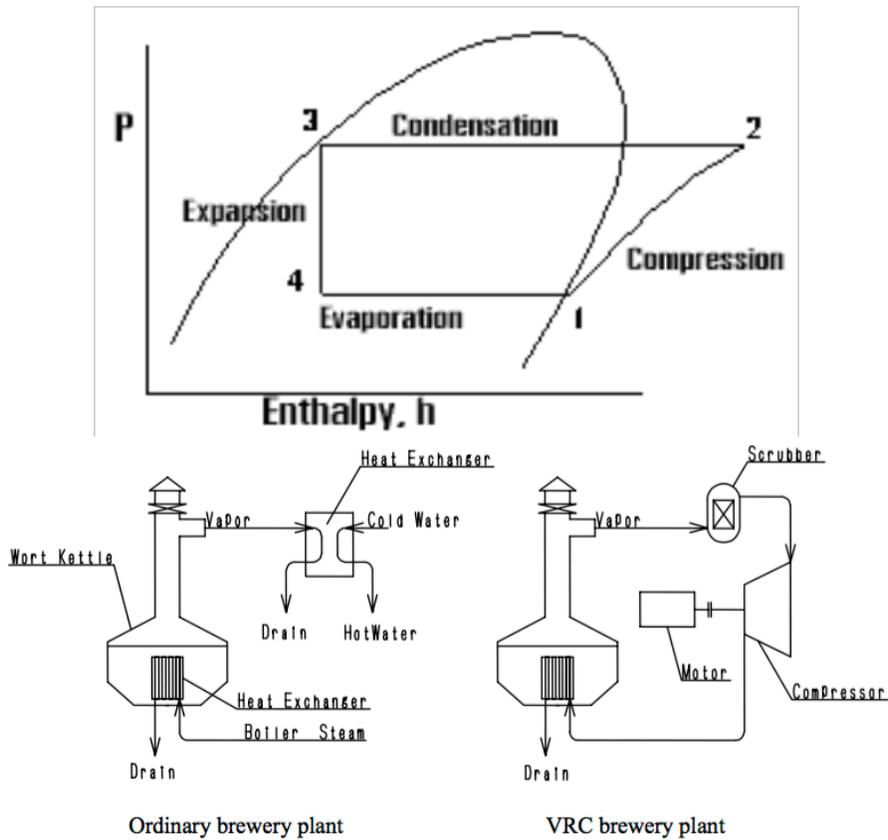


Fig.1 Ordinary Brewery plant and VRC Brewery plant

For a typical brewery the mashing process (heating of the mash, produced from water and grain to produce liquid wort) accounts for 20% of the energy consumption of the plant. Energy recovery from this process is a simple way to cut costs at a brewery. On the left of Fig. 1, above, is depicted the ordinary process of heat exchange for steam produced in the mashing process. To the right a vapor recompression (VRC) system is shown.

In the VRC system, the wort/mash boiler (called a mash tun) releases saturated steam at 120°C. After isothermal scrubbing, a mechanical vapor recompressor (MVR) produces superheated steam at 4.00 MPa and 700°C.

- a) Calculate the work needed to run the compressor.
- b) What is the efficiency of this compressor?
- c) If this steam is then condensed to saturated liquid (2 to 3 in the pressure/enthalpy plot shown above) what heat can be added to the mash?
- d) This arrangement of a compressor used to heat steam is often compared to a heat pump. Calculate the coefficient of performance for this process as a heat pump. What is the comparable coefficient of performance for a Sterling or Carnot heat pump? Explain the difference.

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	State	T°C	P MPa	S kJ/kg-K	H kJ/kg
1	Sat. V	120	0.199	7.13	2710
2	SHS	700	4.00	7.62	3910
2'	SHS	514	4.00	7.13	3480 (isentropic)
3	Sat. L	250	4.00	2.80	1090
4	L/V	120	0.199		1090 (isoenthalpic from P vs H plot)

a) $W_{EC} = 1200 \text{ kJ/kg} = 3910 \text{ kJ/kg} - 2710 \text{ kJ/kg}$

b) Assume adiabatic so $S_2' = 7.13 \text{ kJ/kg-K}$. At $P = 4.00 \text{ MPa}$

$$T_2' = 500^\circ\text{C} + 50^\circ\text{C} * (7.13 \text{ kJ/kg-K} - 7.09 \text{ kJ/kg-K}) / (7.23 \text{ kJ/kg-K} - 7.09 \text{ kJ/kg-K})$$

$$= 500^\circ\text{C} + 50^\circ\text{C} * 0.286 = 514^\circ\text{C}$$

$$H_2' = 3450 \text{ kJ/kg} + 0.286 * (3560 \text{ kJ/kg} - 3450 \text{ kJ/kg}) = 3480 \text{ kJ/kg}$$

$$W_{EC} = 3480 \text{ kJ/kg} - 2710 \text{ kJ/kg} = 770 \text{ kJ/kg}$$

$$\eta_\theta = 770 \text{ kJ/kg} / 1200 \text{ kJ/kg} = 0.642$$

c) $Q_H = 1090 \text{ kJ/kg} - 3910 \text{ kJ/kg} = -2820 \text{ kJ/kg}$

d) Calculate the coefficient of performance for this as a heat pump.

$$Q_C = \Delta H = 2710 \text{ kJ/kg} - 1090 \text{ kJ/kg} = 1620 \text{ kJ/kg}$$

$$\text{COP} = Q_H / W = 2820 \text{ kJ/kg} / 1200 \text{ kJ/kg} = 2.35$$

$$\text{COP Carnot/Sterling Heat Pump} = (700^\circ\text{C} + 273^\circ\text{K}) / (700^\circ\text{C} - 120^\circ\text{C}) = 1.69$$

Carnot heat pump should have the maximum COP. It doesn't because the heat Q_H includes the heat of vaporization (condensation) of the original steam. That is, this is not a full cycle. The water would have to be boiled to return to the original saturated steam at 120°C . $\Delta H_{v,120^\circ\text{C}} = 2,200 \text{ kJ/kg}$ from the steam table. The actual COP for a cyclic process is,

$$\text{COP}_{\text{cyclic process}} = (2820 \text{ kJ/kg} - 2200 \text{ kJ/kg}) / 1200 \text{ kJ/kg} = 0.517$$

This is the "free heat" that we are taking advantage of in the VCR system, almost half of the heat returned to the "mash tun".